

Turbine

### **Chapter Three**

### **Air Standard Cycles and their Analysis**

**Course Instructor** Dr. Khalaf I. Hamada Assistant Professor

#### **Assumptions of Thermodynamic Cycles Analysis**

<u>Air-standard analysis</u> is a simplification of the real cycle that includes the following assumptions:

- 1) Working fluid consists of fixed amount of air (ideal gas)
- 2) Combustion process represented by heat transfer into and out of the cylinder from an external source.
- 3) Differences between intake and exhaust processes not considered (i.e. no pumping work)
- 4) Engine friction and heat losses not considered

### **Carnot Heat Engine**

$$\eta_{th} = \frac{W_{cycle}}{Q_{in}} = \frac{Q_{in} - |Q_{out}|}{Q_{in}} = 1 - \frac{|Q_{out}|}{Q_{in}}$$
$$\eta_{th,Carnot} = \frac{W_{cycle}}{Q_{in}} = \frac{Q_{in} - |Q_{out}|}{Q_{in}} = 1 - \left(\frac{|Q_{out}|}{Q_{in}}\right)_{rev}$$



#### **Carnot's Theoretical Model for Steam Engine**

Kelvin and Rankine suggested that,

$$\left(\frac{|Q_{out}|}{Q_{in}}\right)_{rev} = \frac{T_L}{T_H}$$

Temperatures must be on the absolute scale!

Therefore, the thermal efficiency of a Carnot Heat Engine is,



## SI Engine Cycle vs Air Standard Otto Cycle



# **Air-Standard Otto cycle**

- 1. Process  $1 \rightarrow 2$  Isentropic compression
- 2. Process  $2 \rightarrow 3$  Constant volume heat addition
- 3. Process  $3 \rightarrow 4$  Isentropic expansion
- 4. Process  $4 \rightarrow 1$  Constant volume heat rejection









$$R = \frac{P_2 v_2}{T_2} = \frac{P_1 v_1}{T_1} \rightarrow \boxed{\frac{P_2}{P_1} = \frac{T_2}{T_1} \cdot \frac{v_1}{v_2}}$$

2→3 Constant Volume Heat Addition

$$(u_3 - u_2) = \left(+\frac{Q_{in}}{m}\right) - \frac{W}{m}$$
$$\frac{Q_{in}}{m} = (u_3 - u_2)$$
$$w = \frac{P_2}{RT_2} = \frac{P_3}{RT_3} \rightarrow \boxed{\frac{P_3}{P_2} = \frac{T_3}{T_2}}$$



 $3 \rightarrow 4$  Isentropic Expansion

$$(u_4 - u_3) = \frac{\cancel{Q}}{m} - (+\frac{W_{out}}{m})$$



$$\frac{v_4}{v_3} = r$$



$$\frac{P_4 v_4}{T_4} = \frac{P_3 v_3}{T_3} \rightarrow \boxed{\frac{P_4}{P_3} = \frac{T_4}{T_3} \cdot \frac{v_3}{v_4}}$$

#### 4 → 1 Constant Volume Heat Removal





#### **First Law Analysis**

Net cycle work:

$$W_{cycle} = W_{out} - W_{in} = m(u_3 - u_4) - m(u_2 - u_1)$$

Cycle thermal efficiency:

$$\eta_{th} = \frac{W_{cycle}}{Q_{in}} = \frac{W_{out} - W_{in}}{Q_{in}} = \frac{(u_3 - u_4) - (u_2 - u_1)}{(u_3 - u_2)}$$

$$\eta_{th} = \frac{(u_3 - u_2) - (u_4 - u_1)}{u_3 - u_2} = 1 - \frac{u_4 - u_1}{u_3 - u_2}$$

### **Cold Air-Standard Analysis**

• For a cold air-standard analysis the specific heats are assumed to be constant evaluated at ambient temperature values ( $k = c_p/c_v = 1.4$ ).

• For the two isentropic processes in the cycle, assuming ideal gas with constant specific heat using  $Pv^k = const$ . Pv = RT yields:

$$1 \rightarrow 2: \qquad \frac{T_2}{T_1} = \left(\frac{v_1}{v_2}\right)^{k-1} = r^{k-1} \qquad \frac{T_2}{T_1} = \left(\frac{P_2}{P_1}\right)^{\frac{k-1}{k}}$$
$$3 \rightarrow 4: \qquad \frac{T_4}{T_3} = \left(\frac{v_3}{v_4}\right)^{k-1} = \left(\frac{1}{r}\right)^{k-1} \qquad \frac{T_4}{T_3} = \left(\frac{P_4}{P_3}\right)^{\frac{k-1}{k}}$$
$$\eta_{th}_{const c_v} = 1 - \frac{c_v (T_4 - T_1)}{c_v (T_3 - T_2)} = 1 - \frac{T_1}{T_2} = \left[1 - \frac{1}{r^{k-1}}\right]$$

#### **Effect of Specific Heat Ratio**



Cylinder temperatures vary between 20K and 2000K where 1.2 < k < 1.4

# **Thermodynamic Cycles for CI engines**

- In early CI engines the fuel was injected when the piston reached TDC and thus combustion lasted well into the expansion stroke.
- In modern engines the fuel is injected before TDC (about 20°)



- The combustion process in the early CI engines is best approximated by a constant pressure heat addition process → **Diesel Cycle**
- The combustion process in the modern CI engines is best approximated by a combination of constant volume & constant pressure → **Dual Cycle**

## Early CI Engine Cycle vs Diesel Cycle



### **Air-Standard Diesel Cycle**

- Process  $1 \rightarrow 2$  Isentropic compression
- Process  $2 \rightarrow 3$  Constant pressure heat addition
- Process  $3 \rightarrow 4$  Isentropic expansion
- Process  $4 \rightarrow 1$  Constant volume heat rejection



### **First Law Analysis of Diesel Cycle**

Equations for processes  $1 \rightarrow 2$ ,  $4 \rightarrow 1$  are the same as those presented for the Otto cycle



 $Q_{in}$ 

 $3 \rightarrow 4 \text{ <u>Isentropic Expansion</u>}$  $(u_4 - u_3) = \frac{\cancel{P}}{m} - (+\frac{W_{out}}{m})$  $\boxed{\frac{W_{out}}{M} = (u_3 - u_4)}$ 

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Note that 
$$v_4 = v_1$$
, so:  $\frac{v_4}{v_3} = \frac{v_4}{v_2} \cdot \frac{v_2}{v_3} = \frac{v_1}{v_2} \cdot \frac{v_2}{v_3} = \frac{r}{r_c} \rightarrow \frac{v_4}{v_3} = \frac{r}{r_c}$ 

$$\frac{P_4 v_4}{T_4} = \frac{P_3 v_3}{T_3} \longrightarrow \frac{P_4}{P_3} = \frac{T_4}{T_3} \cdot \frac{r_c}{r}$$

### **Thermal Efficiency**

$$\eta_{Diesel} = 1 - \frac{Q_{out}/m}{Q_{in}/m} = 1 - \frac{u_4 - u_1}{h_3 - h_2}$$

For cold air-standard the above reduces to:

$$\eta_{\substack{Diesel\\const c_{v}}} = 1 - \frac{1}{r^{k-1}} \left[ \frac{1}{k} \cdot \frac{\left(r_{c}^{k} - 1\right)}{\left(r_{c} - 1\right)} \right] \quad \text{recall}, \quad \eta_{Otto} = 1 - \frac{1}{r^{k-1}}$$

Note the term in the square bracket is always larger than one so for the same compression ratio, *r*, the Diesel cycle has a *lower* thermal efficiency than the Otto cycle

When  $r_c (=v_3/v_2) \rightarrow 1$  the Diesel cycle efficiency approaches the efficiency of the Otto cycle



The cut-off ratio is not a natural choice for the independent variable A more suitable parameter is the heat input, the two are related by:

$$r_{c} = 1 - \frac{k - 1}{k} \left( \frac{Q_{in}}{P_{1}V_{1}} \right) \frac{1}{r^{k-1}} \quad \text{as } Q_{in} \rightarrow 0, r_{c} \rightarrow 1 \text{ and } \eta \rightarrow \eta_{Otto}$$

### Modern CI Engine Cycle vs Dual Cycle



### **Dual Cycle**

Process  $1 \rightarrow 2$  Isentropic compression

Process  $2 \rightarrow X$  Constant volume heat addition

Process  $X \rightarrow 3$  Constant pressure heat addition

Process  $3 \rightarrow 4$  Isentropic expansion

Process  $4 \rightarrow 1$  Constant volume heat rejection





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### **Thermal Efficiency**



where 
$$r_c = \frac{v_3}{v_x}$$
 and  $\alpha = \frac{p_3}{p_2}$ 

Note, the Otto cycle ( $r_c=1$ ) and the Diesel cycle ( $\alpha=1$ ) are special cases:

$$\eta_{Otto} = 1 - \frac{1}{r^{k-1}} \qquad \eta_{Diesel} = 1 - \frac{1}{r^{k-1}} \left[ \frac{1}{k} \cdot \frac{(r_c^k - 1)}{(r_c - 1)} \right]$$

#### **Comparison between Otto, Diesel and Dual cycles**

The use of the Dual cycle requires information about either:

i) the fractions of constant volume and constant pressure heat addition

(common assumption is to *equally* split the heat addition), or

- ii) maximum pressure  $p_3$ .
- iii) Transformation of  $r_c$  and  $\alpha$  into more natural variables yields

$$r_{c} = 1 - \frac{k - 1}{\alpha k} \left[ \left( \frac{Q_{in}}{p_{1}V_{1}} \right) \frac{1}{r^{k-1}} - \frac{\alpha - 1}{k - 1} \right] \qquad \alpha = \frac{1}{r^{k}} \frac{p_{3}}{p_{1}}$$

For the same inlet conditions  $p_1$ ,  $V_1$  and the same compression ratio:

$$\eta_{Otto} > \eta_{Dual} > \eta_{Diesel}$$

For the same inlet conditions  $p_1$ ,  $v_1$  and the same peak pressure  $p_3$  (actual design limitation in engines):

$$\eta_{Diesel} > \eta_{Dual} > \eta_{otto}$$

For the same compression ratio

 $\& p_{I_{.}} V_{I}$ :



For the same peak pressure  $p_3$ 

 $\& p_{1.} V_{1}$ :

# **Type of Fuel Vs Combustion Strategy**

• Highly volatile with High self Ignition Temperature: Spark Ignition. Ignition after thorough mixing of air and fuel.

• Less Volatile with low self Ignition Temperature: Compression Ignition, Almost simultaneous mixing & Ignition.